

The final exam is comprehensive but will concentrate on the material since the first exam. 10-2-03 - Topic Coverage for Exam I, Ma4261.

- multivariate calculations for general random variables - review of multiple integration
 - marginals, conditionals, independence
 - covariance, correlation
 - mgfs
 - best mean square prediction
- special distributions
 - binomial, multinomial, negative binomial
 - Poisson rvs and Poisson process
 - gamma (exponential and chi square too)
 - * waiting times
 - * squares of standard normals
 - the bivariate normal, prediction intervals
- transformations and sampling theory
 - direct calculation for discrete and continuous random variables
 - the transformation method for continuous random variables
 - * Box-Muller
 - * Student's (Gossett's) t- distribution definition and pdf
 - the mgf method
 - * $\frac{\sqrt{n}(\bar{X}-\mu)}{\sigma} \sim N(0,1)$ if X_1, \dots, X_n are iid $N(\mu, \sigma^2)$
 - * $\frac{(n-1)S^2}{\sigma^2} \sim \chi_{n-1}^2$.
 - * $\frac{\sqrt{n}(\bar{X}-\mu)}{s} \sim t_{n-1}$ for a random sample from a normal population
 - application to confidence intervals
 - * for the mean of a normal
 - * for the variance of a normal

Main topics since the first exam -

- order statistics
 - joint density of all the order statistics
 - marginal density of a subset of order statistics
 - * univariate marginals, the uniform distribution, probability transform, and the beta distributions
 - * the multinomial heuristic
 - a distribution-free confidence interval for a population quantile
- limiting distributions
 - convergence in law (or distribution) - definitions and techniques
 - * working directly with convergence of the cdf
 - * using the moment generating function (proof of the central limit theorem)
 - convergence in probability - definitions and techniques
 - * equivalence of convergence in probability to a constant c and convergence in law to the distribution with all mass at c - so the techniques from convergence in law can be used here too
 - * Chebyshev's inequality
 - Slutsky's theorem: $A_n \xrightarrow{p} a, B_n \xrightarrow{p} b, X_n \xrightarrow{L} X$ implies $A_n X_n + B_n \xrightarrow{L} aX + b$; applications to large sample confidence intervals for means and proportions.
- estimation
 - methods of point estimation
 - * Method of moments
 - * Method of maximum likelihood
 - * Bayes method
 - properties of estimators
 - * unbiasedness
 - * consistency
 - interval estimation: review one sample and introduce two sample confidence intervals
- hypothesis testing
 - Simple vs simple
 - * type I and type II error: fix α and minimize β
 - * Neyman-Pearson lemma and applications
 - Composite hypotheses
 - * UMP tests and the Neyman-Pearson lemma for selected examples
 - * non-existence of UMP tests generally (no proof): summary of important and useful "good" hypothesis tests; heuristics behind these tests
 - setting up hypotheses
 - reading and utilizing SAS output from proc ttest